1. Vocabulary (15 points)

Give short (1-2 sentence) definitions for each of the terms below, in a way that explains how the items in each pair of terms differ from each other.

a). declaration vs. initialization
   A declaration notifies the compiler about the type of a particular variable. Initialization is the process of giving the variable an initial value.

b). nested class vs. subclass
   A subclass is created using the keyword extends, and should be used for concepts that refine the base class in some way while keeping its essential nature intact. A nested class is created by placing a class definition within another, and should be used for concepts that depend for their meaning on the context of the surrounding class, but have their own unique structure.

c). assignment vs. allocation
   Assignment refers to the act of giving a value to some variable or field. Allocation refers to the act of reserving memory to store some data. The memory thus reserved may then be used in an assignment to some variable.

d). argument vs. parameter
   An argument is a value provided when a method call is made. A parameter is a special variable defined in the method header that represents a piece of information that must be passed to the method when it is called. When the method is called, the arguments values are assigned to their corresponding parameters.

e). class definition vs. class instance
   The class definition is the piece of code that defines the members of a class – its fields and methods. This definition must occur only once within the program. A class instance is a piece of data that represents one example (possibly one of many) of the set of fields found in the class definition; it may be manipulated using the methods.

2. Stacks (16 points)

Draw the states of the stack during processing of each of the postfix arithmetic expressions below. If an error occurs, draw the states up to the point of the error and explain what happens. The answer to the first one is shown for you as an example.

a). 2 3 +

   2 2 5

b). 3 * 4

   3 3 Error: popped empty stack

c). 9 7 5 – *

   9 7 18

d). 9 7 – 5 *

   9 9 2 2 10

e). 8

   8
3. **Recursion** (14 points)

The program below uses recursion to find the minimal element of an array. Draw a diagram of the memory state for the program below at the point where execution reaches the CHECKPOINT line for the third time. (You do not need to show any stack frames for method invocations that have been completed, but if you do draw them please make sure they are clearly crossed out or erased.) Your program should show the call stack and any storage on the heap that is referenced by call stack variables.

```java
/** Use recursion to find the minimum */
public class RecursiveMin {
    public static double findMin(double[] A, int n) {
        double result;
        if (n == 0) {
            result = Double.POSITIVE_INFINITY;
        } else {
            double minRemainder = findMin(A, n-1);
            if (A[n-1] < minRemainder) {
                result = A[n-1];
            } else {
                result = minRemainder;
            }
        }
        return result; // CHECKPOINT
    }

    public static void main(String[] args) {
        double[] A = {6.0,1.0,9.0,3.0,4.0};
        System.out.println("Minimum element: "+findMin(A,A.length));
    }
}
```

4. **Links** (16 points)

The program below creates several data structures in memory. Draw a diagram of the memory state for the program below at the point where execution reaches CHECKPOINT A, and a second diagram for the point where execution reaches CHECKPOINT B. Your program should show the call stack and any storage on the heap that is referenced by call stack variables.

```java
public class Spaghetti {
    public Spaghetti A;
    public Spaghetti B;

    public static void main(String[] args) {
        Spaghetti f = new Spaghetti();
        Spaghetti g = new Spaghetti();
        Spaghetti h = new Spaghetti();
        f.A = f;
    }
}
```
5. **Lists** (12 points)

Suppose that at a given time, a LinkedList<String> named list is in the state shown. Predict the effect of each of the sequences of commands below and draw the resulting state of the list. (Assume that each subquestion begins with the state shown; they are not sequential.) If an exception will occur, give its name.

a). list.set(2,list.remove(2));

b). ListIterator<String> iter = list.listIterator();
iter.next(); iter.next(); iter.add("F"); iter.next(); iter.add("G");

c). ListIterator<String> iter = list.listIterator(list.size());
iter.previous(); iter.previous(); iter.remove(); iter.next(); iter.remove();

6. **Sorting** (12 points)

Each diagram below shows some snapshots of the state of memory for one of the sorting algorithms we have studied. (The states are shown in sequence with the earliest at the top, but not all states are shown.) Identify the algorithm used in each case.

a). Insertion sort. Elements are taken from the unsorted list in the order they appear, and inserted in the sorted list at the correct point.

b). This is Quicksort. It recursively sorts an array in place.

c). Selection sort. The unsorted list is searched for the smallest remaining element, which is then removed and added to the end of the sorted list.
Consider the three methods shown below. Analyze the running time of each in terms of \( n \), where \( n \) is the number of elements in \( s \), under the assumption that class \texttt{List} is (i) actually a \texttt{LinkedList}, or (ii) actually an \texttt{ArrayList}. Justify each analysis with an argument. If the method will generate an exception, state what it would be.

The outer while loop below executes \( n \) times. All operations inside it are constant time for the LinkedList, so the whole thing is \( O(n) \). For an ArrayList the add() method may trigger a copy as the list grows, so it is technically \( O(n) \), making the entire loop \( O(n^2) \). However, if the total size of the ArrayList was specified in advance, then the add() is constant-time, and the whole loop would thus be \( O(n) \).

```java
public <T> void pickRandomly1(List<T> s, List<T> t) {
    ListIterator<T> pos = s.listIterator();
    while (pos.hasNext()) {
        T item = pos.next();
        if (Math.random() > 0.5) {  // 50% chance
            t.add(item);
        }
    }
}
```

The outer while loop below executes \( n \) times. For a LinkedList, remove() is \( O(n) \) because it has to traverse the list to find the index given. This would make the whole thing \( O(n^2) \). However, the code will trigger a ConcurrentModificationException because modifying \( s \) via remove() invalidates the iterator. The ArrayList would also be \( O(n^2) \) but has the same exception problem.

```java
public <T> void pickRandomly2(List<T> s, List<T> t) {
    ListIterator<T> pos = s.listIterator();
    while (pos.hasNext()) {
        pos.next();
        if (Math.random() > 0.5) {  // 50% chance
            t.add(s.remove(pos.previousIndex()));
        }
    }
}
```

The outer while loop below executes \( n \) times. For a LinkedList, get() is \( O(n) \) because it has to traverse the list to find the index given. This makes the whole thing \( O(n^2) \). The ArrayList would be \( O(n) \) if sufficient space has been allocated in advance, or \( O(n^2) \) if the add() call triggers copying into a larger array.

```java
public <T> void pickRandomly3(List<T> s, List<T> t) {
    for (int i = 0; i < s.size(); i++) {
        int j = (int)Math.floor(Math.random()*s.size());  // random index
        t.add(s.get(j));
    }
}
```